## Correlated phenotypic transitions to competence in bacterial colonies

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Genetic competence is a phenotypic state of a bacterial cell in which it is capable of importing DNA, presumably to improve survival under stress. Motivated by several colony-level known responses, we present a model for the influence of quorum sensing on the transition to competence of B. Subtilis. Coupling to the external signal creates an effective inhibitory mechanism, which results in anticorrelation between the cycles of adjacent cells. We show that this is consistent with recent experimental measurements and propose measurement methods to verify the role of quorum-sensing signals.

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Genetic competence is a differentiation process in which bacterial cells (such as those of *Bacillus Subtilis*) synthesize a specific system of proteins for the binding and uptake of DNA [1]. Internalizing exogenous DNA leads to genetic transformations, increasing survival probability [2]. Under certain environmental conditions, a population of genetically identical cells (grown in homogeneous and identical environments) will at a given time be composed of two distinct subpopulations, a competent minority versus a noncompetent majority, each with distinguished features. This has often been attributed to bistability [3–5] in the genetic regulatory network responsible for the competent state, and indeed the necessary positive feedback has been found in the dynamics of one of the key regulatory molecules (comK) [6,7].

More recently, Elowitz and co-workers [7,8] have proposed that the competence transition is reversible and that a competent cell will return to its vegetative state after a characteristic time. This means that one should think of the network as being excitable [9], with stochasticity (perhaps due to small molecular numbers) occasionally driving quiescent cells into the excited competent state. This result represents one of the first examples where the inherent stochasticity of genetic networks [10-13] is being put to functional use. One consequence of this picture is that the competent subpopulation is not fixed but rather is continually fluctuating. Surprisingly, they have also claimed that this transition is made on the single-cell level and is uncorrelated among different cells. This is supported by the measurement of the competence excursion times of neighboring cells. But in this work we show that this may not be the right parameter to measure if quorum sensing is to be studied. The purpose of this paper is to present a putative quorum-sensing mechanism that induces short-ranged spatial anticorrelations between cells and to suggest the appropriate way to experimentally detect such a mechanism. In this scenario, a cell becoming competent will bias its neighbors against making the same choice. Yet excursion times remain uncorrelated as obtained experimentally. Our work is motivated by the many recently discovered instances in which signaling between bacterial cells [14] is used to create colony-level collective responses to external environmental challenges [15,16]. For instance, it is clear that the sporulation response in bacillus is spatially coordinated [17]. At the end, we will discuss experimental tests of our predictions.

We start by considering the molecular interactions underlying the competence circuit ([18], see also Fig. 1). The onset of competence is stimulated by cell crowding and nutrient limitation. Detection of cell crowding is achieved by cell-cell signaling; various molecules are secreted and sensed by the cells to monitor population density (quorum sensing) as well as other environmental conditions. In B. Subtilis, the competence and sporulation factor (CSF) is a diffusible peptide, derived from the PhrC pheromone, which is secreted by the cells during growth. As its extracellular concentration increases due to cell crowding, the CSF is transported back into the cell [19,20] where it influences a cascade of several genes, leading eventually to either sporulation or competence, depending on its concentration. For low concentrations (but above the transport threshold) it (indirectly) enhances the phosphorylation of ComA, and consequently the expression of ComS. ComS competes with ComK for degradation by the MecA-ClpC-ClpP complex, thereby causing an indirect activation of ComK by ComS. ComK activates the transcription of several genes that encode DNA transport proteins and is considered as the indicator for the competent state. ComK activates its own expression and indirectly inhibits the expression of ComS. This double positive feedback loop can, as already mentioned, lead to a bistable responsei.e., two possible states with different gene expression. The negative feedback loop governs the escape from the competent state, as ComK degradation increases when ComS production is inhibited.

In Refs. [7,8] a model was proposed for the part of the circuit downstream from the external signal transducer ComA. Specifically, they proposed

$$\frac{\partial K}{\partial t} = a_K + \frac{b_K K^n}{K_0^n + K^n} - \frac{K}{1 + K + S},$$
$$\frac{\partial S}{\partial t} = \frac{b_S K_1^p}{K_1^p + K^p} - \frac{S}{1 + K + S} + \eta(t), \tag{1}$$

where *K* and *S* represent the concentrations of the ComK and ComS proteins.  $a_K$  (+ $b_K$ ) represent the minimal (fully activated) rates of ComK production, and  $K_0$  is the concentration of ComK required for 50% activation. The cooperativities of ComK autoactivation and ComS repression are parametrized



FIG. 1. (Color online) (a) Schematic representation of the competence circuit in B. Subtilis. Solid lines represent direct interaction; dashed lines represent indirect interaction. (b) Time development of a colony of cells. Color code represents the ComK level, from low ComK level (vegetative state, black) to high ComK level (competent state, white). Adjacent cells rarely become competent simultaneously, due to effective mutual inhibition.

by the Hill coefficients n=2 and p=5. Similarly, the expression of ComS has maximum rate  $b_S$  and is half-maximal when  $K = K_1$ . Degradation by the MecA complex affects both ComK and ComS; the nonlinear degradation term corresponds to such a competitive mechanism. Random fluctuations in ComS expression are represented by a noise term  $\eta(t)$ . Degradation rates of K and S are normalized to unity and are assumed to be identical. The parameters can be chosen to give rise to an excitable system where there exists a stable fixed point plus two other intersections of the K-S nullclines: a saddle point and an unstable fixed point. [This case is presented in Fig. 2(a), where we also show a typical trajectory for which the noise has caused a large excursioni.e., has excited the competent state.] Eventually the cell returns to the vegetative stable state, due to the repression of ComS by ComK; when the value of S decreases below a threshold level, K is more rapidly degraded and can no longer autoactivate its production. One can obtain similar results with more biologically realistic noise forms [4,8,21].

In this model, each cell was taken to be independent of the other cells. This assumption cannot be completely correct, however, since the external enabling signal acting through ComA comes from the rest of the colony. Obviously, the functional utility of having a competent subpopulation would clearly be enhanced if this subpopulation were spatially dispersed. In order to consider the possible spatial effect of quorum sensing, we introduce an extension of the model, and take into account a putative biological mechanism [see Fig. 1(a)], in which the basal production level of ComS depends on a quorum-sensing pheromone Q. The motivation for this particular model is a microarray analysis [22] which has shown that the gene Spo0A, which is upstream of the PhrC secretion mechanism, is down regulated when ComK is high. Thus, the secretion of the CSF, which is a regulator for competence onset, is effectively inhibited by ComK. Specifically, we assume that

$$\frac{\partial S}{\partial t} = c_S Q(x,t) + \frac{b_S K_1^p}{K_1^p + K^p} - \frac{S}{1 + K + S} + \eta(t).$$
(2)

Now K and S are functions of space as well as time, and Q depends on the cells' state in the following manner:

$$\frac{\partial Q}{\partial t} = \frac{1}{2} \tanh[A(K_{max} - K) + 1] + D\nabla^2 Q - \delta_Q Q. \quad (3)$$

The production of Q is maximal as  $K \rightarrow 0$ —namely, normal growth—and it decreases as the cell becomes competent.  $K_{max}$  is chosen to be the threshold value of K, used to define the competent state. Q diffuses with coefficient D and is degraded with a constant rate  $\delta_Q$ . The parameters are chosen to describe a bistable system for Q=1, an excitable system for Q close to but less than 1 and a monostable one if  $Q \ll 1$ . In fact, for the system described in Fig. 2(a), a Q level as low as 0.9 is sufficient to drive the system to the vegetative monostable regime [see Fig. 2(b)]. This is a key point, as very small changes in the external signal (e.g., the level of CSF) may drive the cell into a completely different regime. Therefore, even a twofold change in the Spo0A production and in the resulting secretion of the CSF may have a substantial effect on a possible competence transition.

Our goal in this model is a semiquantitative evaluation of correlations in the competence status of nearby cells. We will study this question in one spatial dimension (with periodic boundary conditions), with a cell at every one of the 5000 grid points. In each explicit time step, the values of K and S are updated for each cell and then Q is updated in the entire space.

A typical simulation run of our model starting from all vegetative cells is shown in Fig. 1(b). There are clear anticorelations between cells, due to the effective inhibition created by a reduction of Q emission by the competent cells. To get a more quantitative measure, we measured the spatial correlation function

$$C_d(i) = \frac{\langle [K_i(t) - \bar{K}_i] [K_{i+d}(t) - \bar{K}_{i+d}] \rangle}{\sigma_i \sigma_{i+d}}, \qquad (4)$$

where we average over time,  $\sigma$  is the standard deviation, and the subscript refers to a specific cell *i*. We then average over all cells *i* to obtain an estimate  $\overline{C}_d$ . In Fig. 3(a) we present the function  $C_1$ —i.e., the correlation between adjacent cells versus the diffusion coefficient of the quorum-sensing pheromone Q. For a small diffusivity, the inhibiting effect is negligible as the diffusion length is small compared to the intercell distance. As D is increased, the mutual inhibition is increased and the correlation is negative, as expected. The maximal effect on nearest neighbors is when the characteristic length  $\lambda = \sqrt{D\tau}$ , given by the diffusivity and the degradation time  $\tau = \delta_0^{-1}$ , is comparable to the intercellular distance. For the given parameters, the maximal effect on adjacent cells—i.e.,  $\lambda = 1$ —is obtained for D = 1. For an intercellular distance of 1  $\mu$ m, the highest mutual inhibition on nearest neighbors will be obtained for  $D=1/\tau$  ( $\mu$ m<sup>2</sup>/s). However, noticeable effects might still exist for faster diffusion, depending on the feedback strength and on whether there are barriers to diffusive transport.



FIG. 2. (Color online) Phase planes diagram for the ComK-ComS system [Eqs. (1) and (2)]. Null clines are presented for ComK (blue, thick dark) and ComS (green, thick gray), and the system fixed points. (a) The excitable system, obtained from Eqs. (1) and (2) with the parameters a=0.004,  $b_K=0.08$ ,  $b_S=0.8$ ,  $k_0=0.2$ , and  $k_1=0.222$ . The noise rms amplitude is 3.5 and  $\Delta t=0.01$ . The fixed points are (from left to right) a stable point, as addle point, and an unstable point. A characteristic trajectory is presented (thin black line) for a single cell, starting from the vegetative state (low ComK). (b) The monostable system, for Eq. (3) and Q=0.9,  $b_s=0.6$ ,  $c_s=0.2$ , and  $\delta_Q=1$ ,  $D_Q=1$  [other parameters as in (a)]. The only fixed point refers to the vegetative state.



FIG. 3. (Color online) (a) Correlation between ComK values of adjacent cells as a function of diffusivity. The mutual inhibition, as identified by negative correlation, vanishes for small diffusivities as well as for large diffusivities. (b) Cumulative histograms of differences between excursion times, of the entire colony (solid line) and adjacent cells (markers).

In the experimental data of [7], sister cells showed no correlation between their excursion times, once they become competent. This led to the assumption that there was no important spatial coupling. However, this conclusion might be inaccurate, as there might be correlations between the cycles of neighboring cells but not between their excursion times. In our simulations, excursion times only slightly changed with the diffusion coefficient (about 10%-data not shown). And no correlation was observed between the excursion times of neighboring cells, as can be seen in Fig. 3(b), which is very similar to the results of [7]. However, there are notable correlations in the times of competence onset of neighboring cells, as demonstrated in Fig. 3(a). This occurs because the Q field has little effect on the competent state itself, but is required to be high for the noise-induced excitation. Therefore, the excursion time measurement is misleading and does not definitively indicate whether there is, or there is not, a quorum-sensing mechanism which influences the competence transition. Clearly, our predictions could be tested within the same experimental framework.

The existence of diffusing inhibition in this system suggests that under certain circumstances the colony should be able to support a patterned Turing state consisting of periodically repeating regions of competent and noncompetent cells. There are two distinct possibilities: the system might have a Turing instability which eliminates the vegetative state completely or it might be multistable, meaning that patterned states coexist with the uniform one. Analysis revealed that no Turing instability exists in this system, but multistability can exist for large enough diffusion constant. In Fig. 4 we consider the temporal evolution of a colony with an initial stripe pattern, in which every tenth cell is competent. It should be noted that such a pattern cannot spontaneously appear, as the uniform vegetative state is always stable. The values of the relevant parameters are chosen to be  $a_k=0.004$ ,  $b_k=0.14$ ,  $k_0=0.2, b_s=0.58, k_1=0.222$ , and  $c_s=0.1$ . For these values the K-S system of equations is bistable for Q=1 and vegetative monostable for Q < 0.6. When the diffusion of Q is slow



[Fig. 4(a)], the local decrease in Q shifts the local *K-S* system of each competent cell to the monostable, vegetative state, the cells revert to vegetative, and the pattern vanishes. But when diffusion is faster [Fig. 4(b)], the averaged value of Q can lie above the monostability threshold and the pattern is stable.

We can get a better understanding of the stripe pattern and of the lack of a Turing instability by explicitly evaluating the Q field. If we approximate the tanh in Eq. (3) as a step function, we find that, in steady state,

$$Q(x) = 1 - \frac{1}{2\sqrt{D\delta_Q}} \sum_{i} \exp\left(-\sqrt{\frac{\delta_Q}{D}}|x - x_i|\right), \quad (5)$$

where the sum ranges over competent cells. This geometric series can easily be calculated for any specific x; the result is shown in Fig. 4(c) as compared to the simulation data. We see that the pattern is possible only because the self-inhibition is weakened sufficiently by the diffusion so as to allow the competent sites to remain in the bistable range. Paradoxically, the competent cells are the most inhibited, which is presumably why this pattern would not spontaneously appear from the uniform vegetative state. Studying this experimentally would necessitate preparing the system with

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FIG. 4. (Color online) A striped colony of cells simulation results. The cell state is represented by color code, from vegetative (white) to competent (black). (a) For D=1, the stripe pattern is unstable and the cells return to their vegetative state. (b) For D=2, the stripe pattern is stable. (c) The steady-state profile of Q(x), analytic solution (solid line) and simulation results (asterisks).

an externally imposed pattern of CSF and then determining whether the pattern remains in place even after the external pattern is removed.

To summarize, we present a model for collective behavior of a colony of B. Subtilis cells. The condition of each cell is described by the concentrations of two proteins: ComK and ComS. The dynamics is described by a set of two rate equations, with a double-feedback loop. The production rates effectively depend on the cell density in the entire colony, sensed by a diffusible pheromone. This pheromone is likely to depend on the protein ComK. This additional mechanism creates an effective inhibition between neighboring cells, leading to anticorrelation in the cells competent-vegetative cycles. Excursion times of neighboring cells are found to be uncorrelated, due to the self-excitatory mechanism of ComK, also in agreement with experimental results. These findings can be experimentally verified by the direct measurement of ComK concentration in the cells, as was done in Ref. [7] via fluorescence techniques.

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